2016 James S. Rickards Fall Invitational

For all questions, answer choice (E) NOTA means that none of the given answers is correct. Also, for this test, $0^0 = 1$. Good Luck!

1.	What is the number	ber of distinct arrangements of the word POKEMONGO?			
	(A) 362880	(B) 181440	(C) 120960	(D) 81000	(E) NOTA

2. Let A stand for an angle of a triangle, and S stand for a side of a triangle. Which of the following is NOT a way to prove triangle congruency?

- (A) AAS (B) SSS (C) ASA (D) SSA (E) NOTA 3. Simplify $\sqrt{2 + \sqrt{2 + \sqrt{2 + \dots}}}$ (A) 2 (B) 4 (C) 3 (D) $2\sqrt{2}$ (E) NOTA
- 4. What is the sum of the real solutions of $(x^2 + 4x + 4)^{x+2} = 1$? (A) -6 (B) -4 (C) -5 (D) -3 (E) NOTA

5. How many edges does a polyhedron with 120 faces and 62 vertices have? If you are wondering, this polyhedron is called a disdyakis triacontahedron.
(A) 180
(B) 182
(C) 184
(D) 186
(E) NOTA

6. Let x be directly proportional to y and inversely proportional to the square of z. If x is 3 when y is 7 and z is 4, what is y when z is 5 and x is 2? (A) $\frac{48}{175}$ (D) $\frac{175}{175}$ (D) $\frac{175}{175}$

(A)
$$\frac{46}{7}$$
 (B) $\frac{60}{7}$ (C) $\frac{173}{24}$ (D) $\frac{173}{36}$ (E) NOTA

7. Nihar is playing darts on a square dartboard defined by 4 lines: y = 0, y = 5, x = 0, and x = 5. To score a point, Nihar has to hit the dartboard above the line y = 2x. If Nihar throws 3 darts, what is the probability that he scores 2 or more points?

(A) $\frac{1}{2}$ (B) $\frac{1}{4}$ (C) $\frac{3}{8}$ (D) $\frac{5}{32}$ (E) NOTA

8. What is the shortest distance between the point (12, 5) and the line y = 5x + 17? (A) $\frac{36\sqrt{26}}{13}$ (B) $\frac{72\sqrt{26}}{13}$ (C) $\frac{72\sqrt{13}}{13}$ (D) $\frac{48\sqrt{13}}{13}$ (E) NOTA

9. How many trailing zeroes does 2016! have? (A) 500 (B) 502 (C) 504 (D) 506 (E) NOTA

10. What is the units digit of $2016^{2016} + 2015^{2015} + 3^{12345} + 7^{54321}$? (A) 5 (B) 3 (C) 1 (D) 7 (E) NOTA

- 11. What is $\sin(30^{\circ})\cos(60^{\circ})\tan(45^{\circ})$? (A) $\frac{3}{4}$ (B) $\frac{1}{4}$ (C) $\frac{\sqrt{3}}{4}$ (D) $\frac{\sqrt{2}}{8}$ (E) NOTA
- 12. If x + y = 10 and $x^2 + y^2 = 50$, what is $x^3 + y^3$? (A) 100 (B) 150 (C) 200 (D) 250 (E) NOTA
- 13. Which of these 4 points is NOT on Euler's line?
(A) Incenter(B) Circumcenter(C) Orthocenter(D) Centroid(E) NOTA

14. Find the sum of the two abscissas and 2 times both of the ordinates of the intersection of the following equations:

- 15. What is the converse of the inverse of the contrapositive of the statement, "If you are a nerd, then you play Pokemon GO."?
 - (A) "If you aren't a nerd, then you don't play Pokemon GO."
 - (B) "If you don't play Pokemon GO, then you aren't a nerd."
 - (C) "If you are a nerd, then you play Pokemon GO."
 - (D) "If you play Pokemon GO, then you are a nerd."

(E) NOTA

16. Find the remainder when $5x^6 + 7x^5 - x^4 + 12x^3 - 4x^2 + 6$ is divided by x - 1. (A) -13 (B) 20 (C) 25 (D) (D) 30 (A) - 13(E) NOTA

17. Compute the area of the convex polygon with vertices at the points (0,0), (3,4), (2,7), (-3,5), and (-6,1). (A) 71 (B) $\frac{71}{2}$ (C) $\frac{21}{2}$ (D) $-\frac{21}{2}$ (E) NC (E) NOTA

- 18. The operation & is defined as $a\&b = \frac{a^2}{b} + \frac{b^2}{a}$. Find (1&3) · (4&2). (A) 84 (B) 87 (C) 80 (D) 86 (E) NOTA
- 19. What is the sum of the elements of the first 12 rows of Pascal's Triangle if the first row has 1 element? (A) 8191 (B) 4095 (C) 8190 (D) 4094 (E) NOTA

20. If you are picking letters from a bag that has the letters A-J in it with replacement, what is the expected number

- of times you would need to draw a letter before you have picked one of each letter? (A) 10 (B) $\frac{275}{7}$ (C) $\frac{9901}{252}$ (D) $\frac{495}{120}$ (B) $\frac{275}{7}$ (D) $\frac{4951}{126}$ (E) NOTA
- 21. What is the sum of the coefficients of the expansion of $(w + 3x + 7y 9z)^6$? (B) 2 (C) 64 (D) 729 (A) 1 (E) NOTA
- 22. Find the determinant of the following matrix: $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 2 & 1 & 0 & 3 \\ 3 & 5 & 2 & 1 \\ 9 & 3 & 7 & 4 \end{bmatrix}.$ (A) 88 (B) - 88(C) 86 (D) - 86(E) NOTA
- 23. Mr. Harrington leaves his house to go walk in a forest. He leaves his house and walks 6 miles west, 10 miles north, $4\sqrt{2}$ miles southeast at a 45° angle, 10 miles west, and 3 miles north. How far away is he from his house? All answers are given in miles. (C) $\sqrt{215}$ (D) $5\sqrt{10}$ (A) 15 (B) 20(E) NOTA
- (D) $\frac{31}{12}$ (E) NOTA

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25. Find $\frac{1}{2} + \frac{2}{4} + \frac{2}{4}$ (A) 2	$\frac{3}{8} + \frac{4}{16} + \frac{5}{32} + \dots$ (B) e	(C) 3	(D) π	(E) NOTA
26. Solve for <i>x</i> : log (A) 2	$g_2 x + \log_4 x + \log_{16} x + \log_2 (B) 4$	$_{256} x + \ldots = 6.$ (C) 8	(D) 16	(E) NOTA
27. Suppose \sqrt{A} + (A) 30	$\sqrt{B} = \sqrt{8 + \sqrt{60}}.$ Find A^2 (B) 64	$(C) 60^{2} + B^{2}.$	(D) 34	(E) NOTA
28. How many pos(A) 36	itive integral factors does 2 (B) 72	016 have? (C) 3	(D) 8	(E) NOTA
29. What is the dis (A) $2\sqrt{3}$	stance between the foci of t (B) $4\sqrt{3}$	he conic section $x^2 + 4y^2$ (C) $2\sqrt{6}$	x - 2x + 16y = 15? (D) $4\sqrt{6}$	(E) NOTA
30. What is $3 + \frac{3}{3} $	$\frac{4}{+rac{4}{3+rac{4}{-}}?}$			

(A)
$$\frac{3}{4}$$
 (B) $\frac{4}{3}$ (C) 3 (D) 4 (E) NOTA